Effect of Calcium Nitrate on the Vapor-Liquid Equilibria of Ethanol + Water and 2-Propanol + Water

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The effect of calcium nitrate on the vapor-liquid equilibria of ethanol + water and 2-propanol + water was studied using a Swietoslawski ebulliometer. The measurements were performed for two constant salt molalities (1 and 2 mol·kg⁻¹) under isobaric conditions at 50.66 kPa. Strong salting-out of the alcohol was observed in all cases, leading to a complete elimination of the azeotropic point at relatively low salt concentrations. The results were correlated using an extension of the NRTL equation for mixed solvent electrolyte systems proposed by Mock, Evans, and Chen.

Introduction

The vapor-liquid equilibrium (VLE) behavior of solvent mixtures may be strongly influenced by the presence of salts. In water + alcohol systems usually an increase of the concentration of the alcohol component in the vapor phase compared to the salt-free system is observed (salting-out), which in many cases results in a shifting or complete elimination of azeotropic points. Therefore, salts have been used as separating agents in extractive distillation as an interesting alternative to solvents (1, 2). For the design of separation processes involving salt components an accurate description of the VLE behavior is necessary. However, in many cases the required experimental information is not available. Little is known about the effect of calcium nitrate on the VLE equilibrium of alcohol + water systems. The data of Rius Miro and Alvarez Gonzales (3, 4) were measured only for the salt-saturated system and do not cover the whole range of liquid composition in the case of the system 2-propanol + water + calcium nitrate. In order to decide to what extent the azeotropic point is shifted at lower salt concentrations, the VLE equilibrium of the systems ethanol + water + calcium nitrate and 2-propanol + water + calcium nitrate was measured at constant salt molalities of 1.0 and 2.0 mol·kg⁻¹.

 Table 1. Interaction Parameters and Nonrandomness

 Factors for the NRTL Electrolyte Model

| solvent + solvent (salt) pair | $\alpha_{1,2}^{a}$ | $	au_{1,2}^{a}$ | $	au_{2,1}^{a}$ |
|-----------------------------------|--------------------|-----------------|-----------------|
| ethanol(1) + water(2) | 0.3 | -0.134 | 1.822 |
| 2-propanol (1) + water (2) | 0.3 | -0.131 | 2.587 |
| water (1) + Ca $(NO_3)_2$ (2) | 0.2 | 9.159 | -4.892 |
| $(1) + Ca(NO_3)_2(2)$ | 0.888 (f) | 1.936 (f) | 6.530 (f) |
| 2-propanol (1) + $Ca(NO_3)_2$ (2) | 0.734 (f) | 2.361 (f) | 1.760 (f) |

 $^{a} f = fitted.$

Experimental Section

Equipment and Procedures. Equilibrium compositions and boiling points were measured using a modified Swietoslawski ebulliometer. A detailed description of the apparatus is given by Rogalski et al. (5, 6). The pressure was maintained constant at 50.66 kPa controlled by a Vacuubrand vacuum controller CVC 24 and a Wallace & Tiernan mercury gauge with a resolution of ± 0.01 kPa. Equilibrium temperatures were measured using a calibrated thermometer with an accuracy of ± 0.1 K.

At the beginning of each experimental series, the ebulliometer was charged with an aqueous solution of calcium nitrate of the desired molality. The change of the liquidphase composition was achieved by gradually adding an



Figure 1. Experimental and calculated x'-y and $\vartheta - x', y$ diagrams for ethanol + water + calcium nitrate at 50.66 kPa (salt molality $m = 1.038 \text{ mol·kg}^{-1}$): (Δ , \Box), experimental, (—) calculated, (- -) salt-free system (calculation based on the UNIQUAC equation; parameters taken from Gmehling (10)).

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Figure 2. Experimental and calculated x'-y and $\vartheta - x', y$ diagrams for ethanol + water + calcium nitrate at 50.66 kPa (salt molality $m = 2.049 \text{ mol·kg}^{-1}$): (Δ , \Box), experimental, (-) calculated, (- -) salt-free system (calculation based on the UNIQUAC equation; parameters taken from Gmehling (10)).

Table 2. Vapor-Liquid Equilibrium Data for Ethanol (1) + Water (2) + Ca(NO₃)₂ at 50.66 kPa ($m = 1.038 \oplus 0.001$ mol·kg⁻¹)

| x1'a | У1 | ୬/°C | $\Delta y_1{}^b$ | ∆ϑ°/°C |
|-------------------------|-------|-------|------------------|--------|
| 0.000 | 0.000 | 83.0 | 0.000 | -0.03 |
| 0.003 | 0.044 | 81.8 | 0.003 | -0.27 |
| 0.008 | 0.114 | 79.8 | 0.013 | -0.81 |
| 0.014 | 0.183 | 77.9 | 0.022 | -1.19 |
| 0.021 | 0.241 | 76.0 | 0.022 | -1.55 |
| 0.032 | 0.316 | 73.9 | 0.026 | -1.66 |
| 0.045 | 0.364 | 72.1 | 0.011 | -1.59 |
| 0.061 | 0.429 | 70.5 | 0.019 | -1.40 |
| 0.075 | 0.462 | 69.3 | 0.014 | -1.38 |
| 0.102 | 0.499 | 68.0 | -0.002 | -0.93 |
| 0.135 | 0.541 | 66.9 | -0.004 | -0.60 |
| 0.167 | 0.566 | 66.2 | -0.009 | -0.37 |
| 0.207 | 0.597 | 65.5 | -0.006 | -0.27 |
| 0.317 | 0.651 | 64.4 | -0.004 | -0.22 |
| 0.384 | 0.682 | 64.0 | 0.001 | -0.24 |
| 0.481 | 0.710 | 63.5 | 0.008 | -0.35 |
| 0.548 | 0.754 | 63.3 | 0.008 | -0.34 |
| 0.620 | 0.787 | 63.1 | 0.010 | -0.35 |
| 0.686 | 0.821 | 62.9 | 0.012 | -0.41 |
| 0.768 | 0.862 | 62.8 | 0.010 | -0.38 |
| 0.833 | 0.906 | 62.8 | 0.016 | -0.32 |
| 0.905 | 0.948 | 62.8 | 0.013 | -0.29 |
| 0.975 | 0.986 | 62.8 | 0.004 | -0.31 |
| mean absolute deviation | | 0.011 | 0.66 | |

^a Mole fraction based on the salt-free system: $x_1' = n_1/(n_1 + n_2)$. $n_1, n_2 =$ number of moles of solvents 1 and 2. ^b $\Delta y_1 = y_{1,erp} - y_{1,calc}$. ^c $\Delta \vartheta = \vartheta_{exp} - \vartheta_{calc}$.

alcoholic solution of calcium nitrate of the same molality. In this way the molality of the liquid phase was kept constant over the whole range of solvent composition. However, the withdrawal of salt-free vapor-phase samples results in an increase of the salt to solvent ratio. To maintain a constant salt molality, the mass of each vapor-phase sample was determined using an analytical balance and a corresponding mass of pure alcohol was added to compensate the solvent loss. To obtain results in the alcohol-rich region, the reverse procedure was carried out, adding the aqueous solution to an alcohol + calcium nitrate solution of the same molality. In the case of insufficient solubility of the salt in the pure alcohol, a small quantity of water was added to ensure complete dissolution of the salt.

Measurement of Sample Composition. Liquid- and vapor-phase samples were analyzed using a HP 5890 gas chromatograph with the capillary column technique and

Table 3. Vapor-Liquid Equilibrium Data for Ethanol (1) + Water (2) + Ca(NO₃)₂ at 50.66 kPa ($m = 2.049 \oplus 0.004$ mol·kg⁻¹)⁴

| 101-148 / | | | | |
|-------------------------|------------|-------|--------------|-------|
| <i>x</i> ₁ ′ | <i>y</i> 1 | ϑ/°C | Δy_1 | ∆୬/°C |
| 0.000 | 0.000 | 84.5 | 0.000 | 0.03 |
| 0.002 | 0.047 | 83.1 | 0.012 | -0.54 |
| 0.008 | 0.136 | 80.5 | 0.027 | -1.33 |
| 0.014 | 0.223 | 77.8 | 0.036 | -2.03 |
| 0.023 | 0.301 | 75.4 | 0.041 | -2.40 |
| 0.034 | 0.359 | 73.5 | 0.023 | -2.06 |
| 0.046 | 0.424 | 71.8 | 0.031 | -2.01 |
| 0.062 | 0.473 | 70.3 | 0.022 | -1.58 |
| 0.085 | 0.517 | 68.9 | 0.006 | -0.98 |
| 0.106 | 0.558 | 67.8 | 0.010 | -0.82 |
| 0.138 | 0.577 | 66.9 | -0.013 | -0.33 |
| 0.166 | 0.597 | 66.3 | -0.019 | -0.12 |
| 0.256 | 0.660 | 65.3 | -0.011 | 0.24 |
| 0.325 | 0.685 | 64.9 | -0.016 | 0.29 |
| 0.392 | 0.716 | 64.6 | -0.009 | 0.24 |
| 0.480 | 0.754 | 64.4 | -0.003 | 0.24 |
| 0.579 | 0.790 | 64.2 | -0.006 | 0.21 |
| 0.669 | 0.829 | 64.1 | -0.005 | 0.24 |
| 0.764 | 0.888 | 64.0 | 0.012 | 0.28 |
| 0.840 | 0.928 | 64.0 | 0.014 | 0.37 |
| 0.909 | 0.954 | 64.0 | 0.005 | 0.46 |
| mean absolute deviation | | 0.016 | 0.80 | |
| | | | | |

^a See footnotes a-c in Table 2.

thermal conductivity detector. As the stationary phase of the chromatographic column (25 m \times 0.32 mm) Permabond CW20M (polyethylene glycol 20000) was used. The mesurements were made under isothermal conditions at a column temperature of 70 °C. Hydrogen was used as the carrier gas. In this way vapor- and liquid-phase mole fractions were obtained with an accuracy of ±0.01.

The salt concentration of each liquid phase sample was measured by evaporating the solvent and weighing the dried residue using an analytical balance with a resolution of ± 0.0001 g. The salt molalities proved to be constant within ± 0.004 mol·kg⁻¹. The mean value was found to slightly exceed the concentration of the solution filled into the ebulliometer, which is due to the evaporation of a part of the liquid phase during the operation of the ebulliometer.

Materials. Ethanol and 2-propanol with a guaranteed purity greater than 99.8% were used without further purification. Deionized water was distilled twice. Calcium nitrate tetrahydrate of reagent grade was dried in an electric oven



Figure 3. Experimental and calculated x'-y and $\vartheta - x', y$ diagrams for 2-propanol + water + calcium nitrate at 50.66 kPa (salt molality $m = 1.038 \text{ mol·kg}^{-1}$): (Δ , \Box), experimental, (-) calculated, (- -) salt-free system (calculation based on the UNIQUAC equation; parameters taken from Gmehling (10)).



Figure 4. Experimental and calculated x'-y and $\vartheta - x', y$ diagrams for 2-propanol + water + calcium nitrate at 50.66 kPa (salt molality $m = 2.073 \text{ mol·kg}^{-1}$): (Δ , \Box), experimental, (-) calculated, (- -) salt-free system (calculation based on the UNIQUAC equation; parameters taken from Gmehling (10)).

at 170 °C. The complete removal of water was checked by weighing.

Correlation. The $G^{\rm E}$ model used to correlate the VLE data is an extension of Chen's previously published method for single solvent electrolyte systems to mixed solvent systems (7,8). The basic assumptions about the local composition of an electrolyte solution are (1) repulsion of ions of the same sign, which results in a local mole fraction of zero for cations (anions) surrounding a central cation (anion) and (2) local electroneutrality (the sum of the charges of cations and anions surrounding a central molecule is zero).

The model parameters are specific for solvent-solvent and solvent-salt pairs. For a system containing two solvents, m and w, and one salt, ca, six interaction parameters, $\tau_{m,w}$, $\tau_{w,m,\tau}$, $\tau_{m,ca}$, $\tau_{w,ca}$, $\tau_{ca,m}$, and $\tau_{ca,w}$, and three nonrandomness factors, $\alpha_{m,w}$, $\alpha_{ca,m}$, and $\alpha_{ca,w}$, are required. The parameters for the three binary systems ethanol + water, 2-propanol + water, and water + calcium nitrate were taken directly from Mock et al. (8). The remaining parameters for the binary pairs ethanol + calcium nitrate and 2-propanol + calcium nitrate were estimated by minimization of the following objective function Z using the Simplex-Nelder-Mead method (9): where

$$Z = 100 \sum_{i} g_{i} \left\{ \frac{\vartheta_{\exp} - \vartheta_{calc}}{\vartheta_{\exp}} \right\}^{2} + \sum_{i} g_{i} \left\{ \frac{y_{\exp} - y_{calc}}{y_{\exp}} \right\}^{2} \quad (1)$$
$$i = 1, ..., N_{dp}$$

 ϑ is the temperature (°C) and y the vapor-phase mole fraction. The indices exp and calc denote the experimental and calculated values. N_{dp} is the number of experimental data points and g_i the weighting factor. Boiling points and vaporphase compositions were calculated assuming ideal behavior of the vapor phase and solving the following equilibrium condition iteratively: where x_i is the mole fraction of solvent

$$y_i P = x_i \gamma_i P_i^{s} \tag{2}$$

i in the liquid phase based on the assumption of total dissociation of the electrolyte component In eq 3 the

$$x_i = n_i / (\sum n_{\text{sol}} + \sum n_{\text{ion}})$$
(3)

summation includes the number of moles of solvents and ions present in the liquid phase. The expression for the

Table 4. Vapor-Liquid Equilibrium Data for 2-Propanol (1) + Water (2) + Ca(NO₃)₂ at 50.66 kPa ($m = 1.038 \pm 0.002$ mol·kg⁻¹)^a

| x_{1}' | y_1 | ϑ/°C | Δy_1 | $\Delta \vartheta / ^{\circ} \mathrm{C}$ |
|-------------------------|-------|------|--------------|--|
| 0.000 | 0.000 | 83.0 | 0.000 | -0.03 |
| 0.006 | 0.114 | 79.8 | -0.018 | 0.10 |
| 0.017 | 0.300 | 75.5 | 0.020 | 0.02 |
| 0.027 | 0.380 | 71.9 | 0.019 | -0.99 |
| 0.039 | 0.444 | 69.4 | 0.019 | -1.31 |
| 0.055 | 0.495 | 67.8 | 0.016 | -0.97 |
| 0.072 | 0.536 | 66.9 | 0.021 | -0.53 |
| 0.093 | 0.549 | 66.2 | 0.005 | -0.19 |
| 0.113 | 0.560 | 65.8 | -0.002 | 0.02 |
| 0.141 | 0.572 | 65.5 | -0.007 | 0.20 |
| 0.167 | 0.579 | 65.3 | -0.010 | 0.22 |
| 0.206 | 0.595 | 65.1 | -0.005 | 0.13 |
| 0.243 | 0.603 | 65.0 | -0.005 | 0.03 |
| 0.278 | 0.609 | 64.9 | -0.005 | -0.12 |
| 0.339 | 0.634 | 64.8 | 0.007 | -0.33 |
| 0.407 | 0.654 | 64.7 | 0.009 | -0.55 |
| 0.485 | 0.690 | 64.7 | 0.020 | -0.69 |
| 0.567 | 0.732 | 64.9 | 0.028 | -0.65 |
| 0.639 | 0.768 | 65.1 | 0.029 | -0.63 |
| 0.690 | 0.791 | 65.3 | 0.024 | -0.59 |
| 0.742 | 0.826 | 65.5 | 0.027 | -0.57 |
| 0.778 | 0.852 | 65.7 | 0.029 | -0.52 |
| 0.822 | 0.873 | 65.9 | 0.019 | -0.52 |
| mean absolute deviation | | | 0.016 | 0.43 |

mean absolute deviation

^a See footnotes a-c in Table 2.

activity coefficient of the solvent components γ_i is given by Mock et al. (8). The saturation vapor pressures of the pure solvent components P_i^s were calculated by the Antoine equation using Antoine constants from the literature (10). Table 1 contains the fitted interaction parameters and nonrandomness factors together with the parameters taken from the literature.

Results and Discussion

The experimental results are listed in Tables 2-5 together with deviations between experimental and calculated vaporphase mole fractions and temperatures. As can be seen from Figures 1-4 the addition of calcium nitrate results in a considerable increase of the mole fraction of the alcohol in the vapor phase compared to the salt-free systems. For ethanol + water + calcium nitrate no azeotrope exists even at the lower salt concentration of 1.04 mol·kg⁻¹. The solubility of calcium nitrate in 2-propanol was not sufficient to obtain results at high alcohol content in the case of the 2-propanol + water + calcium nitrate system. The calculated curve for the vapor-phase mole fraction indicates a complete elimination of the azeotropic point.

The calculated vapor-phase mole fractions show satisfactory agreement with the experimental values. However, the errors for the boiling temperatures are rather systematic, leading to

Table 5. Vapor-Liquid Equilibrium Data for 2-Propanol (1) + Water (2) + Ca(NO₃)₂ at 50.66 kPa ($m = 2.073 \pm 0.003$ mol·kg⁻¹)^a

| x1' | У1 | ϑ/°C | Δy_1 | $\Delta \vartheta / {}^{o}C$ |
|-------------------------|-------|------|--------------|------------------------------|
| 0.000 | 0.000 | 84.5 | 0.000 | 0.00 |
| 0.004 | 0.104 | 81.8 | -0.003 | 0.01 |
| 0.010 | 0.248 | 77.9 | -0.027 | -0.73 |
| 0.016 | 0.365 | 74.4 | 0.063 | -1.80 |
| 0.029 | 0.462 | 71.1 | 0.050 | -1.38 |
| 0.040 | 0.519 | 68.8 | 0.049 | -1.57 |
| 0.063 | 0.568 | 67.3 | 0.026 | -0.31 |
| 0.083 | 0.596 | 66.3 | 0.018 | 0.06 |
| 0.106 | 0.619 | 65.8 | 0.014 | 0.50 |
| 0.135 | 0.631 | 65.4 | 0.005 | 0.74 |
| 0.157 | 0.641 | 65.2 | 0.004 | 0.78 |
| 0.246 | 0.678 | 64.9 | 0.014 | 0.56 |
| 0.299 | 0.696 | 64.9 | 0.019 | 0.37 |
| 0.355 | 0.716 | 65.0 | 0.025 | 0.24 |
| 0.418 | 0.737 | 65.1 | 0.028 | 0.09 |
| 0.488 | 0.767 | 65.3 | 0.035 | 0.03 |
| 0.533 | 0.793 | 65.6 | 0.044 | 0.17 |
| 0.591 | 0.825 | 65.9 | 0.052 | 0.27 |
| 0.660 | 0.860 | 66.3 | 0.056 | 0.43 |
| 0.738 | 0.891 | 66.6 | 0.047 | 0.46 |
| mean absolute deviation | | | 0.031 | 0.53 |
| | | | | |

^a See footnotes a-c in Table 2.

greater deviations for the boiling points of the alcohol + salt systems compared to the water + salt systems. It may be assumed that this is partly due to model deficiencies (for example, the assumption of total dissociation of the electrolyte over the whole range of liquid composition) and partly due to the use of interaction parameters taken from the literature, which were originally obtained for a different temperature range. Since the nonrandom two-liquid (NRTL) electrolyte model does not regard any temperature dependence, extrapolation to a different temperature may lead to erroneous results.

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